Definition: The rank of a matrix A, written rank(A) is equal to the maximum number of linearly independent rows of A, or equivalently, the dimension of the row space of A

Theorem The maximum number of linearly independent rows of any matrix A is equal to the maximum number of linearly independent columns of A, Thus the dimension of the rowspace of A is equal to the dimension of the column space of A.